

1.  $\frac{d}{dx} \sin x$  cos x
2.  $\frac{d}{dx} \tan x$  sec<sup>2</sup> x
3.  $\sin \frac{\pi}{6}$   $\frac{1}{2}$
4.  $\frac{d}{dx} \sec x$  sec x tan x
5.  $\cos \frac{\pi}{2}$  0

Sep 19-8:58 AM

### 3.6b Chain Rule

Repeated use of the chain rule. Find the derivatives of:

$g(t) = \tan(5 - \sin 2t)$   $g'(t) = 2 \cdot (-\cos(2t)) \sec^2(5 - \sin(2t))$

$u = 2t$   
 $v = 5 - \sin u$

$f(x) = \sqrt{1 + \sin^2(3x)}$  der of inside der of middle der of outside

$h(x) = (\sin(x^3 + 2x) + \cos(5x))^4$   $4u^3$

$h'(x) = [(3x^2 + 2)\cos(x^3 + 2x) - 5\sin(5x)] \cdot 4(\sin(x^3 + 2x) + \cos(5x))^3$

$+ 5(-\sin(5x))$   
 $5 - \sin(5x)$

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$$y = \sec(\tan(x^3 + x))$$

$$y' = (3x^2 + 1) \sec^2(x^3 + x) \sec(\tan(x^3 + x)) \tan(\tan(x^3 + x))$$

$$y = \sec x \tan(x^3 + x)$$

$$y' = \sec x ((3x^2 + 1) \sec^2(x^3 + x)) + \tan(x^3 + x) (\sec x \tan x)$$

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### Chain Rule for parametric equations

$\frac{dy}{dx} = \frac{dy/dt}{dx/dt}$

slope =  $\frac{dy}{dx}$

Find the tangent to the hyperbola branch defined parametrically by

$x = \sec(t)$   $y = \tan(t)$   $-\frac{\pi}{2} < t < \frac{\pi}{2}$  at  $t = \frac{\pi}{6}$

$x = \sec \frac{\pi}{6} = \frac{2}{\sqrt{3}}$   $y = \tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}$

$\frac{dy}{dt} = \sec^2 t$   $\frac{dy}{dx} = \frac{\sec^2 t}{\sec t \tan t}$

$\frac{dx}{dt} = \sec t \tan t$   $\sec \frac{\pi}{6} = \frac{1}{\cos \frac{\pi}{6}} = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}}$

$\tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}$

$\frac{dy}{dx} = \frac{\sec^2 t}{\sec t \tan t} = \frac{1}{\tan t} = \frac{1}{\frac{1}{\sqrt{3}}} = \sqrt{3}$

slope of tan line  $\tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}$

$y = 2(x - \frac{2}{\sqrt{3}}) + \frac{\sqrt{3}}{3}$

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Find the derivatives:

Radians vs Degrees

$$x^{\circ} = \frac{\pi}{180} x \text{ radians}$$

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